Analysis of Compressed Sensing for Efficient Signal Acquisition and Reconstruction

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Abstract

In a variety of industries, including image processing, signal processing, and communications, compressed sensing (CS) has emerged as a viable technique for effective signal capture and reconstruction. The core idea of CS is the capacity to collect and represent signals with much fewer measurements than conventional Nyquist-Shannon sampling theory demands. With the help of CS, precise signal reconstruction is possible from a heavily subsampled set of measurements by taking advantage of the inherent sparsity or compressibility of many natural signals.Compressed sensing for effective signal capture and reconstruction is examined in this research. The fundamental ideas and mathematical foundation of computational science are introduced first, with an emphasis on the crucial elements of the sensing, sparse representation, and reconstruction methods. We address several measuring techniques and their effects on signal recovery performance, including random sensing matrices and structured sensing matrices.We explore ideas like the Restricted Isometry Property (RIP), coherence, and incoherence requirements as we delve into the mathematical features and theoretical guarantees of CS. We examine the trade-off between the degree of signal sparsity and the quantity of measurements necessary for precise reconstruction, elucidating the constraints and practical considerations of CS-based systems. The examination of compressed sensing for effective signal capture and reconstruction is detailed in this paper. We highlight the promise of CS as a formidable paradigm for getting beyond the drawbacks of conventional signal capture techniques by carefully examining the underlying concepts, mathematical aspects, reconstruction algorithms, and applications. CS has the potential to revolutionise numerous fields and offer up new paths for effective data processing and transmission by Article History Article Received: 25 January 2021 enabling efficient sampling and reconstruction. Keywords: Sampling, Compress sensing, complex network, reconstruction Revised: 24 February 2021 Accepted: 15 March 2021 algorithm, Signal Acquisition

Introduction

Due to the vast number of data involved, signal gathering, transmission, and processing have grown increasingly difficult in the age of information explosion. The Nyquist-Shannon sampling theorem underlies conventional signal acquisition techniques, which call for sample rates proportionate to the signal's bandwidth. However, this strategy frequently results in disproportionate data collecting and storage needs, which restricts the effectiveness and usefulness of signal processing systems. The shortcomings of traditional signal acquisition and reconstruction methods have been addressed, and compressed sensing (CS), often referred to as compressed sensing or sparse sampling, has emerged

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as a possible alternative. The fundamental principle of CS is to collect and reconstruct signals with a much less number of measurements than the Nyquist rate by taking advantage of the intrinsic sparsity or compressibility of the signals. The central discovery of CS is that many interesting natural signals, including biological, audio, and image data, have a sparse representation in some transform domain. Because of sparsity, only a small fraction of the transform coefficients can accurately reflect the signal because the majority of coefficients in the transform domain are close to zero. By directly obtaining and processing these sparse coefficients, CS makes signal acquisition more effective and lessens the need for data storage and transmission.

This work seeks to increase knowledge of effective signal capture and reconstruction approaches by exploring the ideas, mathematical underpinnings, algorithms, and applications of compressed sensing. The knowledge gathered from this study can encourage the creation of new CS-based systems, allowing for more effective data processing, transmission, and storage across a variety of industries, including imaging, communications, and signal processing.

Donoho was the first to introduce the cutting-edge signal capture and processing technique known as compressed sensing (CS) [1,2]. With only a few sparse or compressible measurements, it offers the capacity to precisely recreate the original signal from a representation. In doing so, CS contradicts the widely accepted Nyquist-Shannon sampling theorem, which usually calls for more samples to accurately record the information.Let's have a look at a discrete signal x that can be converted into a matrix y by using a transformation matrix Φ dimensions M x N. In CS, the objective is to accurately reconstruct the original signal x from a smaller set of M observations of the signal y, where M << N. By taking use of the signal x's sparse or compressible representation in a transform domain like the wavelet or Fourier domain, this is accomplished.Compressed sensing can be write as follow:

As a sensing matrix, the matrix is in charge of gathering the measurements of the signal y. It provides a compressed form of the signal by capturing a linear combination of the coefficients or samples. The measurements can be acquired incoherently by properly constructing the sensing matrix Φ , which enables accurate reconstruction even with a much less number of measurements than is typically needed.In CS, a problem of optimisation must be solved in order to rebuild the original signal x from the measured data. To obtain the signal's sparsest or most compressible representation that meets the measurements taken, a variety of techniques, including 11-minimization, basis pursuit, and orthogonal matching pursuit, are frequently used.In order for x to be solvable, it must either be sparse or sparse on some orthogonal bases can be written as per following, that is,

The desecrate wavelet transform can be written using above two equation (1), (2). We have;

$$y = \Phi x = \Phi \Psi s = \Theta s \dots (3)$$

Where, $\Phi\Psi$ the sensor matrix is present. Sensing matrix $\Phi\Psi$ must adhere to the constrained isometric property in order to create x from y.

Significant improvements have been made in CS theory and applications [7,8]. Sensing and reconstruction are the two main essential parts of computational science. A sensing matrix is used in the sensing phase to collect a sparse signal while meeting certain requirements. There are many different random, deterministic, and structured random sensing matrices available. It is common

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practise to use random matrices like the Gaussian and Bernoulli matrices. It also makes use of deterministic matrices like polynomial and chaotic matrices. It's also common to use structured random matrices like Toeplitz and Hadamard matrices. The original signal is recreated using a measurement vector and CS algorithms in the reconstruction phase. Convex optimisation, greedy, and Bayesian algorithms are just a few of the reconstructive CS algorithms that are available. These techniques assist in decompressing the compressed measurements received during the sensing phase to restore the original signal.

In addition to theoretical study, CS has found use in several fields, including data compression, image encryption, and cryptography. In numerous sectors, it has been effective in completing tasks requiring secure communication, effective data representation, and signal processing.

I. Sensing Methodology

Since they are so important to signal sampling and the precision of signal reconstruction, sensing methods have long been a focus of CS research. Without any particular precondition, the sensing phase entails correlating a sparse signal with an appropriate sensing matrix. We will give a brief overview of many sensing techniques in this section.

1. Sparse Sensing Method:

The representation of signals under a redundant dictionary is a crucial topic of research in sparse representation. The creation of sparse dictionaries and the creation of quick and effective sparse decomposition techniques are the two main focuses of current work on the sparse representation of signals under redundant dictionaries.

The emphasis has traditionally been on sparsifying dictionary learning, which entails creating a suitable dictionary and a matrix in order to reduce errors in sparse representation. The sparse representation error is defined as follows using Equation (2):

Sparse representation error = $|| y - \Psi s ||$ (4)

The original signalis represented by y in this equation, the redundant dictionary is indicated by Ψ , and the sparse coefficient matrix is indicated by s. The objective is to determine the sparse coefficient matrix s that, by minimising the sparse representation error, most closely resembles the original signal y.

To efficiently learn or adapt the dictionary Ψ and compute the sparse coefficient matrices s, researchers work to provide effective methods and approaches. These techniques are essential for producing precise and condensed representations of signals under redundant dictionaries, enabling functions in signal processing and analysis like de-noising, compression, and feature extraction.

By incorporating a measurement matrix, the problem of sparse dictionary learning was optimised. The optimisation procedure goes like this:

 $\| s(:,k) \| 0 \le K, \forall k, \Phi = f(\Psi) \dots (5)$

Where, The sparse coefficient matrix s has no effect on either variable A or variable B. The provided sparsity matrix Φ or dictionary determines the sensing matrix, indicated as $\Phi = f(\Psi)$. To solve the related optimization challenge, the authors additionally provided an improved measurement matrix and a fresh algorithm.

2. Compress Block Sensing Method:

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Block-compressed sensing (BCS) is a simple method for gathering and compressing data. It can be used to take advantage of its tremendous advantages when working with high-dimensional images and films. In BCS, the image is broken up into a number of tiny patches, and the measurement and reconstruction processes are performed independently on each patch. With this method, the computational complexity is reduced and the sensing matrix's storage needs are much reduced.

The BCS measurement matrix is compact, which allows for effective storage. Once they are obtained, the measurement values of each image patch can be delivered separately. Real-time performance is made possible by the receiver's ability to independently recreate each image patch using the data it has received.

Consider a picture with N = Irx Ic pixels overall and dimensions N= Ir x Ic. The image is partitioned into B x B subblocks, each of which is sampled using the same sensing matrix. The i-th block's vectorized signal is denoted by the symbol xi. You can write the matching output CS vector yi as:

Where, Φ is a block diagonal matrix.

3. Random Compressed Sensing:

The pseudorandom behaviour of the chaotic sequences produced by chaotic systems makes them suited for use as measurement matrices. Contrary to random-sensing matrices, chaotic systems can generate pseudorandom sequences using specialised techniques in the context of chaotic compressed sensing (CCS), which simplifies the creation of sensing matrices. As an illustration, consider the Chebyshev chaotic system [15]:

The following equations serve as a representation of the Chebyshev chaotic system:

 $x(n+1) = a - b * x(n)^{2} + y(n)....(7)$

y(n + 1) = x(n)(8)

In this system, a and b are system parameters, and x(n) and y(n) are the state variables at time step n. These equations can be repeated starting with the initial conditions to create a pseudorandom sequence. When compared to employing a wholly random matrix, this sequence can subsequently be utilized as a measurement matrix in CCS.

CCS offers effective signal capture and compression by taking advantage of the characteristics of chaotic systems. The pseudorandom behaviour of chaotic sequences can be advantageous over conventional random sensing matrices in a number of domains, including image processing, communications, and signal analysis.

To increase transmission security, chaotic measurement matrices are produced [17]. Numerous factors are involved in these advancements, including chaotic parameters, sampling frequency, and matrix mapping functions. The main benefit is that just the matrix seeds need to be stored, as opposed to the full sensing matrix. The beginning value, the chaotic parameters, the sample start point, and the sampling step are some of these seeds.

The chaotic sensing matrix can be rebuilt using the preserved matrix seeds. The chaotic sensing matrix is defined as follows:

 $\Phi = T\left(S(n0, d, C(z0, \varepsilon))\right).$ (9)

Here, f() stands for the function that creates the matrix based on the saved matrix seeds, and Φ stands for the chaotic sensing matrix. The original chaotic sensing matrix can be precisely

Vol. 70 No. 1 (2021) http://philstat.org.ph DOI: https://doi.org/10.17762/msea.v70i1.2510 recreated by employing the identical seeds throughout both the transmission and reconstruction processes. Since only the seeds must be exchanged between the sender and the receiver, rather not the complete matrix, this method ensures the security of the communication.

4. Deep-learning compressed sensing (DL-CS)

An innovative method called deep-learning compressed sensing (DL-CS) combines the strength of deep learning with compressed sensing techniques. In order to improve the performance of compressed sensing, especially in scenarios involving complex and high-dimensional signals, DL-CS intends to make use of deep neural networks.

Deep neural networks are used in DL-CS to recover signals more precisely and effectively by learning the mapping between compressed measurements and the original signals. Improved reconstruction capabilities are made possible by the network architecture, which is built to take use of the signals' innate structure and sparsity.

In a number of applications, including as image and video compression, medical imaging, and signal denoising, DL-CS has demonstrated promising results. It has benefits including increased reconstruction accuracy, less processing complexity, and the capacity to properly handle non-linear signal models. The field of DL-CS research is dynamic, with ongoing projects concentrating on creating sophisticated network designs, investigating cutting-edge training methods, and expanding the usage of DL-CS for various signal processing applications.

Recent research has focused a lot of attention on the integration of compressed sensing with deep learning. Block compressed sensing (BCS) now has a deep-learning technique thanks to Adler et al. [19]. In their research, the block-based linear perception and nonlinear reconstruction stages were handled by a fully connected neural network. A deep neural network to conduct BCS, processing each block independently in accordance with Equation (9). They suggested a four-layer, completely integrated network architecture.

• Input Layer: The compressed measurements or sensing vectors are input to the input layer.

• Hidden Layers: The input data is processed by the hidden layers, which carry out the necessary computations and transformations. Depending on the particular network design, the number of hidden layers and the number of neurons in each layer may change.

• Output Layer: The output layer creates the sparse coefficient matrix or the reconstructed signal for each block.

In order to simplify sampling calculation and improve the calibre of compressed sensing (CS) reconstruction, a deep-learning-based sparse measurement matrix was devised [20]. The sample subnetwork and the reconstruction subnetwork were the two subnetworks that made up the suggested technique.

It was assumed that block CS, also known as NB, in the sample subnetwork had a block size of B B. Nb = M NB was the formula used to determine each block's measurement size. The sensing matrix's Φ lines, each identified by the index k, were written as follows:

The minimal level is: $J(\Phi) = \nu = \alpha (0 \le \alpha < 1)$

Vol. 70 No. 1 (2021) http://philstat.org.ph $a_{k,i}|a_{k,i}|>\mu$,(12)

5. Sensing using Compressed Semitensors Method:

The constraints of traditional matrix operations are solved by the semitensor product (STP) of matrices [18-20]. The usual matrix multiplication rule that requires identical column and row numbers is broken by the STP theory, which permits matrix multiplication even when the dimensions of two matrices are mismatched. The STP offers a more adaptable and dynamic framework for matrix operations while yet maintaining the fundamental characteristics of regular matrix multiplication.

Assume that v is a column vector with dimension p and that u is a row vector with dimension np. In order to divide u into p equal blocks, referred to as u1, u2,..., up, where each part ui is a row vector of size n, is called a split. What is the definition of the semitensor product n of u and v?

According to this definition, the column vector v is multiplied by each portion ui of the row vector u to produce p sub-products. Concatenating these subproducts results in the semitensor product u n v, which has a dimension of np. When the dimensions of matrices are not exactly compatible, the STP offers a mechanism to execute matrix-like operations, enabling more flexible computations and getting around the drawbacks of conventional matrix multiplication.



Figure 1: Semitensor Matrix Multiplication matrix

The criteria for matrix dimensions are the primary distinction between semitensor matrix multiplication and conventional matrix multiplication as shown in figure 1. In conventional matrix multiplication, the multiplication is only acceptable if the column number of matrix A equals the row number of matrix x. The inner dimensions of the matrices are correctly aligned thanks to this dimension-matching requirement.

The semitensor product (STP) theory, however, overcomes this restriction. It permits matrix multiplication even when the dimension-matching requirement is not met by the two matrices. The

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STP divides a matrix into equal blocks and performs tensor products between related blocks to enable the multiplication of matrices with unequal dimensions. The variety of matrices that can be used in these procedures is increased by the flexibility of the dimensionality.

II. Reconstruction Algorithm

1. Convex-Optimization Algorithm

For signal reconstruction in compressed sensing (CS), convex-optimization methods are essential. These methods attempt to solve an optimisation issue with a convex objective function and convex constraints, recovering the original signal from the compressed measurements.

The basis pursuit (BP) algorithm is a popular convex-optimization approach for computer science. By minimising the L1 norm of the signal under the condition that the measurements are consistent with the sensing matrix, BP looks for the sparsest solution that fulfils the measurements. The BP algorithm uses the signal's assumed sparsity to produce precise and effective reconstruction.

In order to tackle signal approximation, the convex-optimization technique transforms a nonconvex problem into a convex one. Let's assume J(x) is the convex cost that encourages sparsity. In other words, when signal x is highly sparse, the value of J(x) is small. The reconstruction of signal x without noise could be expressed as follows using Equation (5):

Similar to this, the reconstruction procedure is as follows when there is noise:

Equation (15) can be reformulated without constraints as follows, by incorporating the cost function H to penalize the distance between Φx and y:

In convex-optimization techniques, J(x) = ||x|| is usually chosen as the 11-norm of the sparse signal x, and H is subsequently solved.

2. Greedy Algorithm

Through sparse approximation, the greedy iterative-reconstruction technique indirectly addresses the challenge of sparse signal reconstruction while addressing combinatorial optimisation issues. Constrained least-squares estimation is used to reconstruct the signal after iteratively determining the sparse vector's support set. The objective of sparse signal reconstruction is to create the sparsest signal possible from a set of linear measurements, or y. This procedure entails identifying the sparse vector that minimises the sparsity and best fits the measurements. The algorithm gradually improves the signal reconstruction until convergence by iteratively choosing and updating the support set of non-zero coefficients.

 $\min\{|I|_{:y} = \sum \varphi_i x_i\}....(18)$ i \varepsilon I

The greedy iterative-reconstruction approach successfully combines constrained least-squares estimation with sparse approximation through an iterative procedure to reconstruct the original signal from the given measurements. In compressed sensing applications, this method provides a workable alternative for recovering sparse signals.

III. Compressed-Sensing Applications

Data compression, image encryption, cryptography, complex network reconstruction, channel estimation, analog-to-information conversion, channel coding, radar reconstruction, radar remote sensing, and digital virtual asset security and management are just a few of the many fields where compressed sensing has found extensive use. Figure 2 depicts an illustration of a compressed sensing-based data encryption transmission system.

Figure 2: Data encryption and compression can be accomplished simultaneously by a data-



Encryption transmission method based on compressed sensing.

This system makes use of compressed sensing techniques to transmit data securely via encryption. A sensing matrix is used to first compress the original data while still preserving the signal's key information. In order to protect the confidentiality and integrity of the compressed data, encryption algorithms are then used to encrypt it. The encrypted data is decrypted and then reverse-engineered using the reconstruction method and sensing matrix at the receiving end. Since the rebuilt data closely resembles the original signal, accurate recovery of the signal is possible. e^{N}

$$\sum_{t+1}(i) = (1 \qquad e)f(x_t(i)) + \sum_{i} c_{ij}g(x_t(j)), \qquad (19)$$

j=1

This data encryption transmission system offers a secure and effective method for transmitting and protecting sensitive information by utilising the power of compressed sensing. It demonstrates the adaptability and efficiency of compressed sensing methods for dealing with data security.

Vaquer et al. focused on acquiring the scalar flux across the whole issue domain and used compressed sensing to lower the memory requirements of a Monte Carlo simulation [15]. They used a strategy that entailed picking a small sample of non-contiguous particle tallies and conducting partial reconstruction on them. Minimising the total variation norm served as a direction for the reconstruction procedure.

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Figure 3: complex network model based on QR decomposition and compressed sensing

Their strategy's success was shown by the outcomes. In a TRIGA reactor simulation, precise flux maps for both thermal and rapid fluxes were produced with only about 10% of the usual amount of tallies. This notable decrease in memory utilisation demonstrated compressed sensing's potential for enhancing Monte Carlo simulations and enhancing computing efficiency without sacrificing accuracy.

IV. Conclusion

A potent framework for effective signal capture and reconstruction is called compressed sensing (CS). By taking use of the sparsity or compressibility of signals, CS makes it possible to acquire high-dimensional data with fewer measurements, which has a substantial impact on data storage, transmission, and computational complexity.CS enables precise signal recovery from sparse data by utilising suitable sensing matrices and reconstruction techniques. To accommodate various applications and signal models, multiple sensing techniques, such as random, deterministic, and structured random matrices, have been developed. For effective signal reconstruction in CS, convex optimisation methods, greedy iterative reconstruction algorithms, and deep learning techniques have also been used.Deep learning, chaotic systems, and semitensor products have all been combined with CS to further broaden its capabilities and uses. Deep learning-based methods have showed promise in handling complicated data structures and enhancing the quality of reconstructed signals. Chaostic sequences have been used in chaotic compressed sensing as measurement matrices, which has streamlined the development process. Matrix multiplication with unmatched dimensions is now possible thanks to semitensor products, which have overcome the constraints of conventional matrix operations. The use of CS extends to a number of fields, including radar sensing, network reconstruction, channel estimation, image encryption, and data compression. It provides effective methods for strengthening data security, minimising the memory footprint, and enabling real-time processing.

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